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# Response-Time Analysis for Task Chains in Communicating Threads (RTAS'16)

Johannes Schlatow, Rolf Ernst

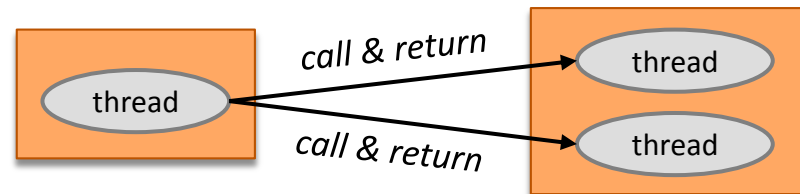
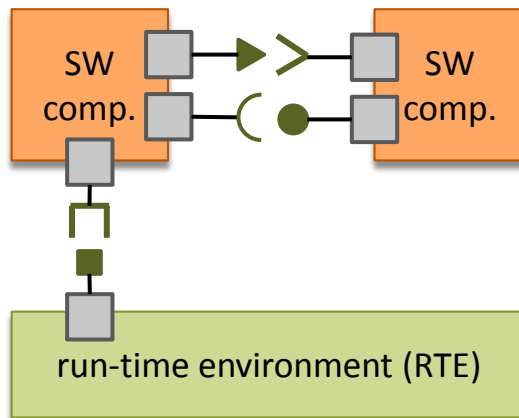
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# Introduction

- growing variety and complexity (e.g. automotive domain)
  - object-oriented and component-based design for reusability and separation (e.g. AUTOSAR)
- interfaces with procedure call semantics (same core) (e.g. microkernel-based systems)



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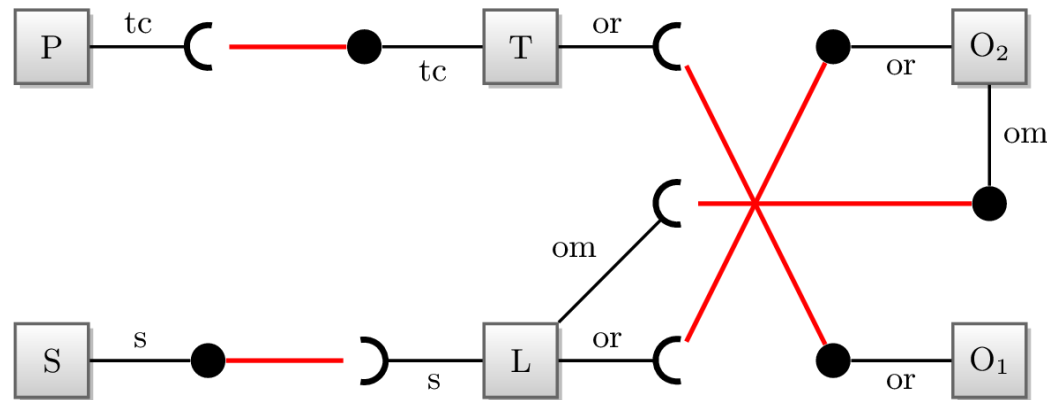


**operating-system (OS) view**

# Motivational example

## Two ADAS functions implemented by multiple software components:

- Parking assistant (P),  
trajectory calculation (T),  
object recognition (O1)
- Lane detection (L),  
object recognition & object masking (O2),  
steering (S)



How can we verify latency requirements of P and L?

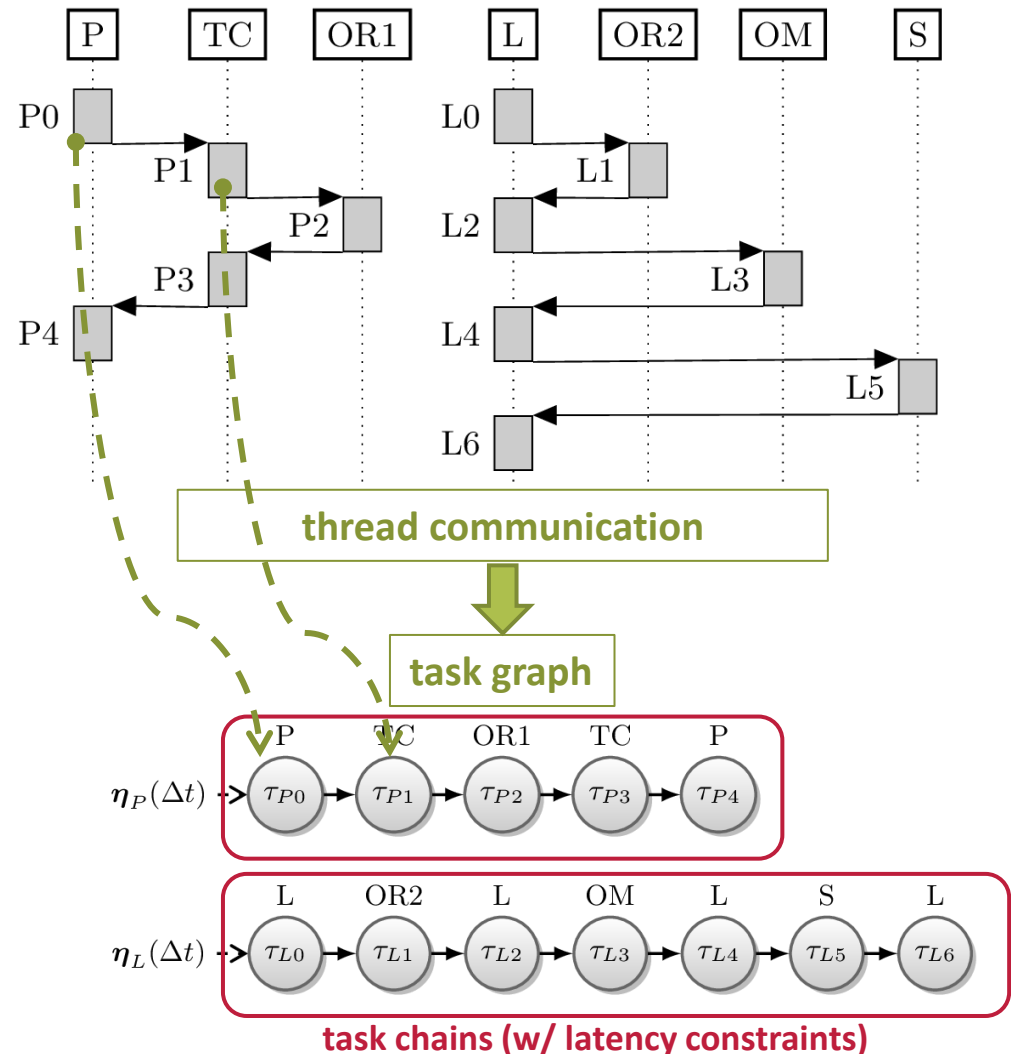
# Modelling communicating threads for timing analysis

## Threads

- sequence of instructions and communication
- scheduled by the OS (here: static priority)
- precedence constraints (dependencies) between thread segments

## Tasks

- activated by preceding task (or external stimulus)
- communicate at completion
- activations can queue up**
- execute on the thread's priority**

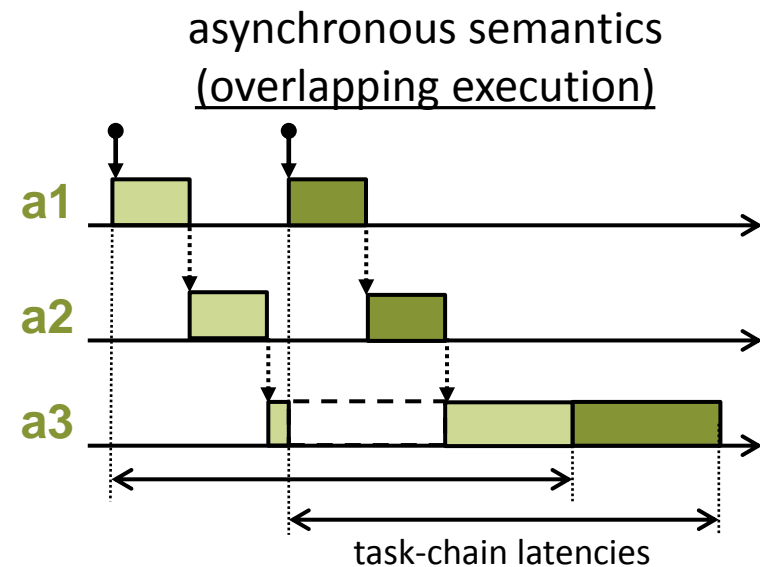
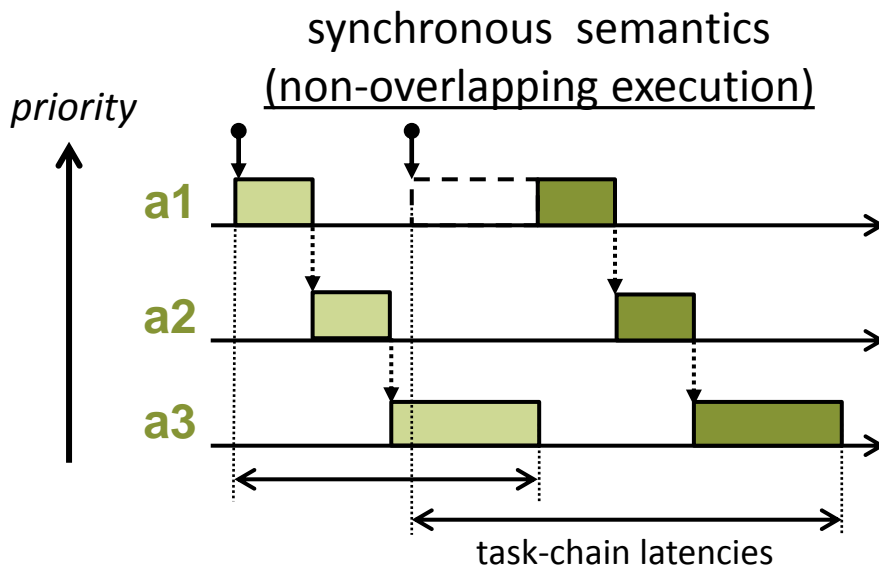
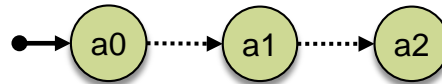


# Observations

## 1. Task graph obfuscates procedure call (synchronous) semantics.

- Caller is blocked until the callee returns
- non-overlapping execution of task chains
- predecessors cannot interfere with dependent tasks (pessimistic results)

Example:



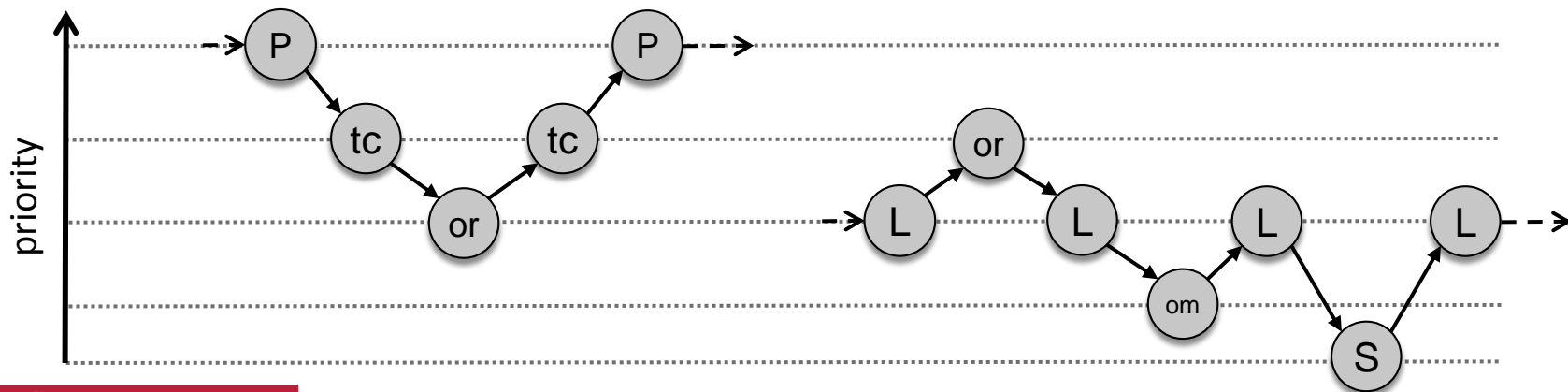
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- in contrast to: descending priority assignment
- task-chain latency = response time of last task



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### Wanted:

### Worst-case latency analysis for task chains on the same resource that...

- considers the procedure call semantics of the thread communication
- can deal with non-monotonic, i.e. arbitrary priority assignments.

# Outline

- Motivation
- Analysis approach and system model
- Response-time analysis for synchronous task chains
- Application to asynchronous task chains
- Related work
- Experimental evaluation
- Conclusion



# Analysis approach – preliminary work

## Analysis flow of Compositional Performance Analysis (CPA)

- **event model interface**  $\eta^{+/-}(\Delta t)$ :  
max/min number of activations between any time window  $\Delta t$
- **local scheduling analysis** based on busy-window technique:  
Calculates amount of time a resource is busy processing  $q$  events of task  $i$ .

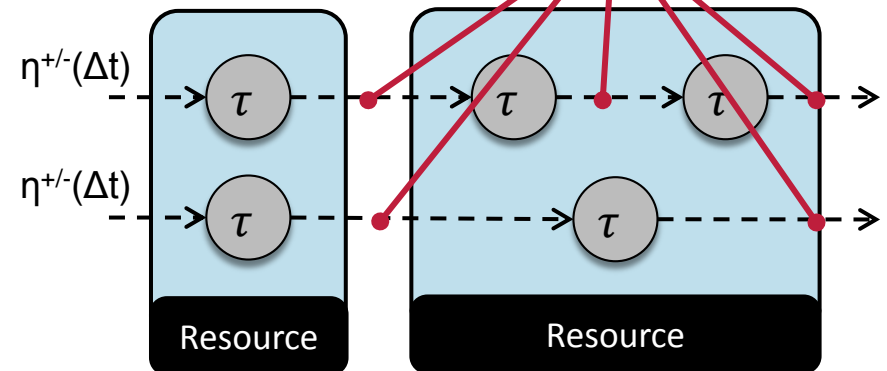
▪ e.g.: 
$$B_i(q) = \underbrace{q \cdot C_i^+}_{\text{core execution time}} + \underbrace{\sum_{j \in I_i} \eta_j^+(B_i(q)) \cdot C_j^+}_{\text{interference from other tasks}}$$

*core execution time*

*interference from other tasks*

**propagation**

- **event model propagation:**  
Derives new event models based on local scheduling analysis results.
- **repeated until convergence**
- **path latency:** sum of WCRTs



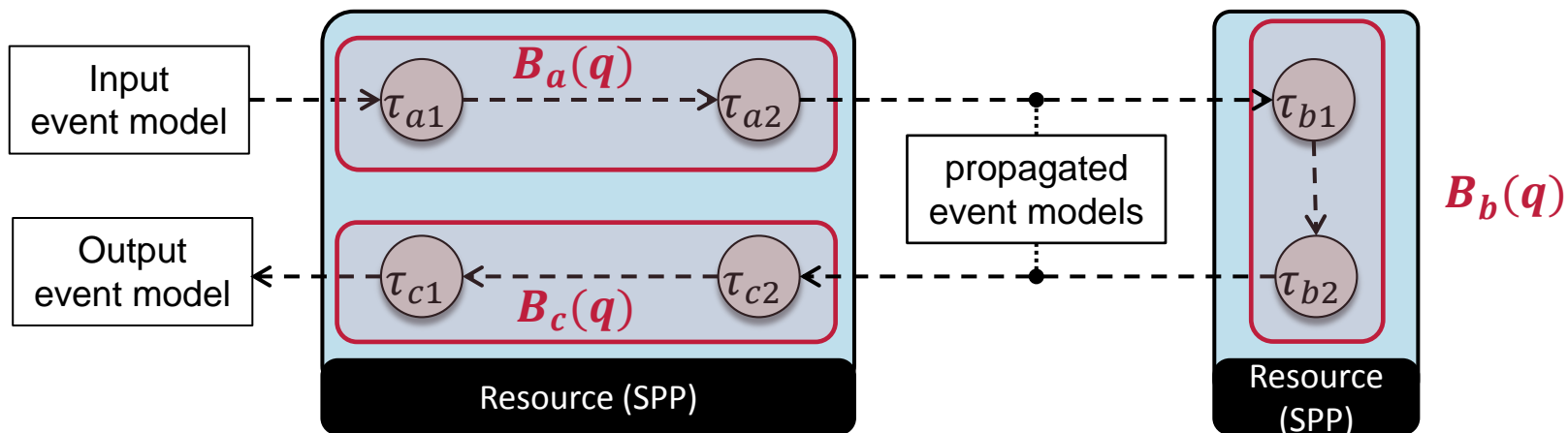
# Analysis approach – modification

**Problem:** Interference accounted multiple times within a task chain.

- Can be limited dependent on the semantics of the task chain.

**Idea:** busy-window analysis for entire task chains

→ **q-event task-chain busy window**



→ **improvement of local scheduling analysis**

→ **applied but not limited to CPA**

# System Model

## Assumptions

- static-priority preemptive (**SPP**) scheduling on processing resource
- task chains do **not cross resource boundaries**
- tasks within the chain have **exactly one incoming and outgoing edge**
- **same communication semantics** for entire resource (easily extensible)
- **arbitrary priorities**

## Terminology

- a task chain  $i$  consists of a **sequence of tasks**  $(\tau_{i1}, \tau_{i2}, \dots, \tau_{in_i})$
- **synchronous** task chain = non-overlapping execution
- **asynchronous** task chain = overlapping execution possible
- **best-case/worst-case execution** time for each job of  $\tau_{ik}$ :  $C_{ik}^-/C_{ik}^+$

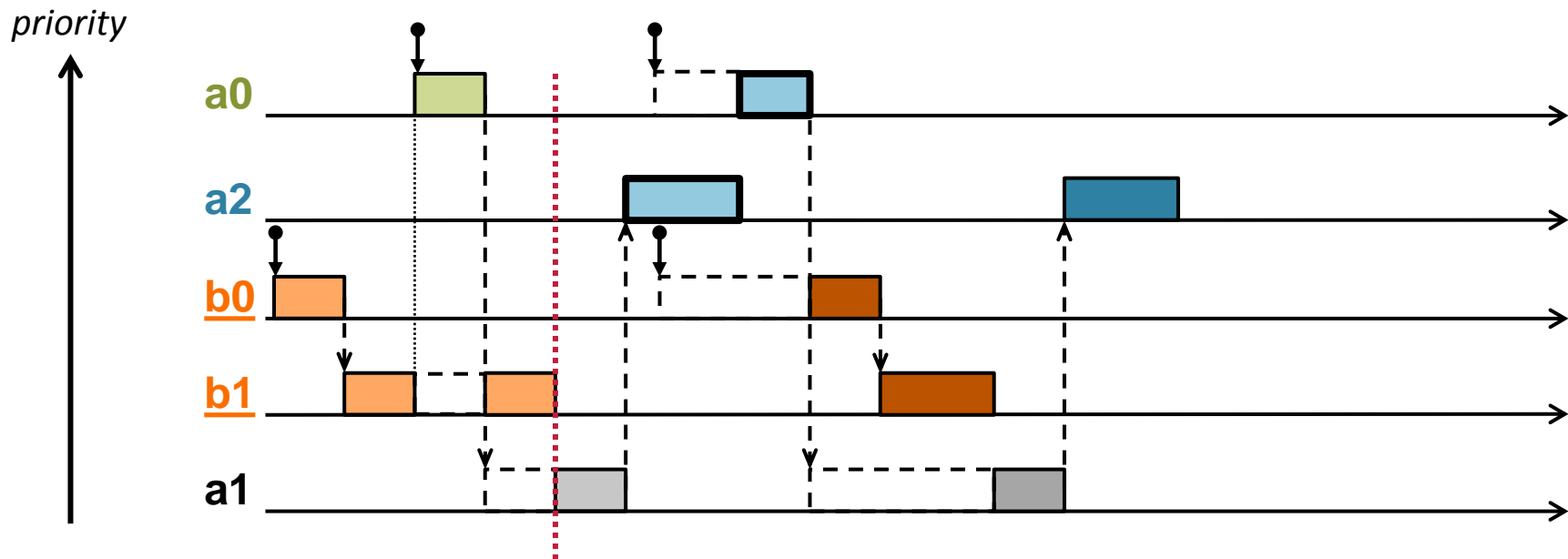
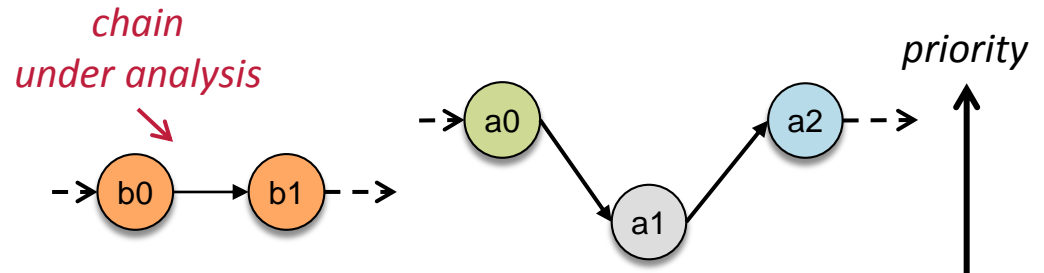
# Response time analysis for synchronous task chains

## Intra-chain interference

- no overlapping execution

## Inter-chain interference

- stalling and **deferred** activations:



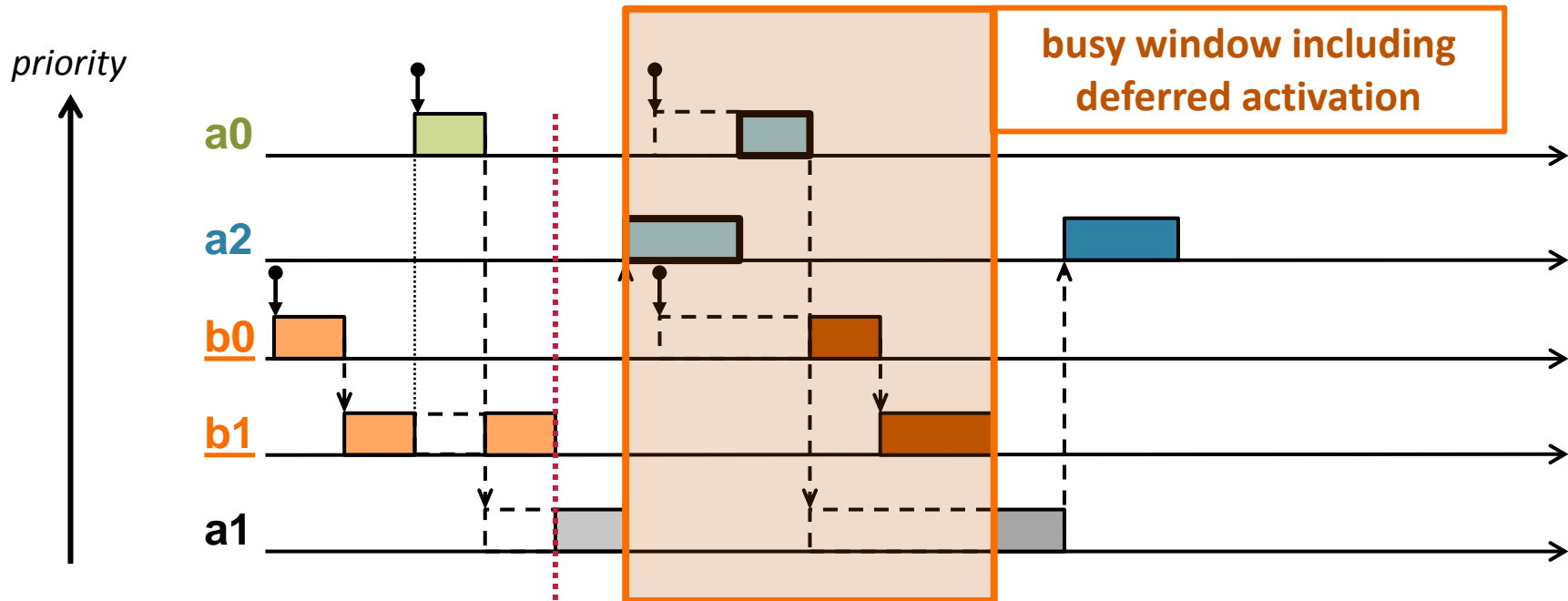
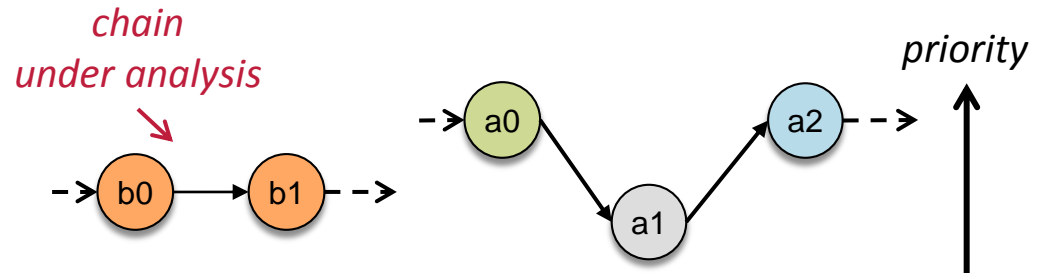
# Response time analysis for synchronous task chains

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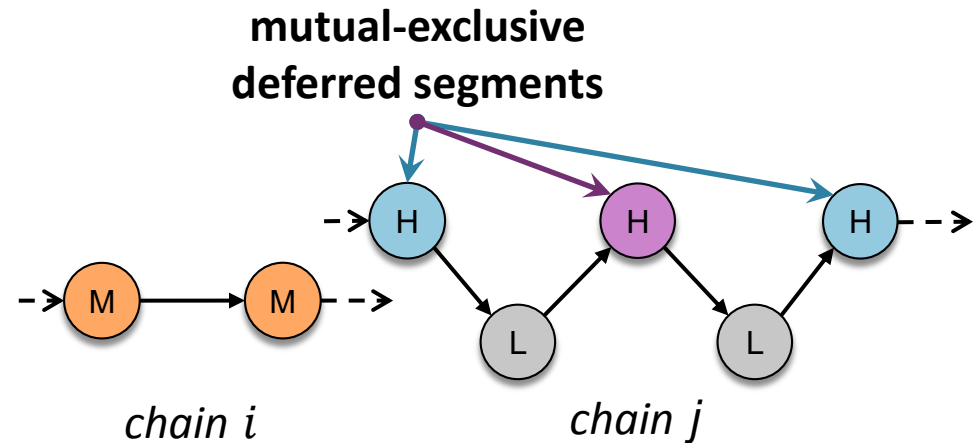
- stalling and **deferred** activations:



# Task-chain busy window for synchronous task chains

## Q-event task-chain busy window:

- self interference bounded by  $q$
- considers every (non-deferred) task on a higher priority than any task in the chain:  $I_{ij}$
- single-time blocking limited to the critical deferred segment  $S_{ij}$



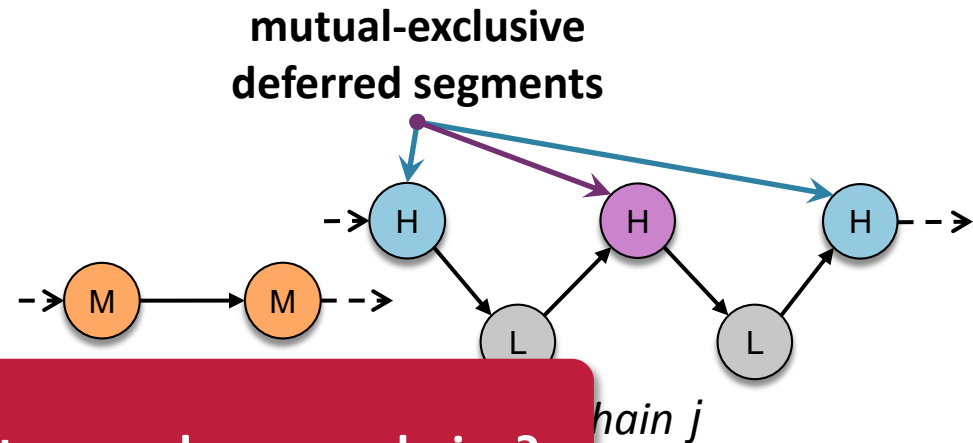
busy-window for task chain  $i$ :

$$B_i(q) = \underbrace{q \sum_k c_{ik}^+}_{\text{self interference (bounded by } q\text{)}} + \underbrace{\sum_{j \neq i} \left( \sum_{j \in I_{ij}} \eta_j^+(B_i(q)) \cdot c_{jk}^+ + \sum_{k \in S_{ij}} c_{jk}^+ \right)}_{\substack{\text{inter-chain} \\ \text{interference}}} \underbrace{\quad}_{\substack{\text{normal interference} \\ \text{(bounded by } \eta_a^+ \text{)}}} \underbrace{\quad}_{\substack{\text{critical} \\ \text{deferred segment}}}$$

# Task-chain busy window for synchronous task chains

## Q-event task-chain busy window:

- self interference bounded by  $q$
- considers every (non-deferred) task on a higher priority than any task in the chain:  $I_{ij}$
- single-time block critical deferred



Can this be applied to asynchronous chains?

busy-window for task chain  $i$ :

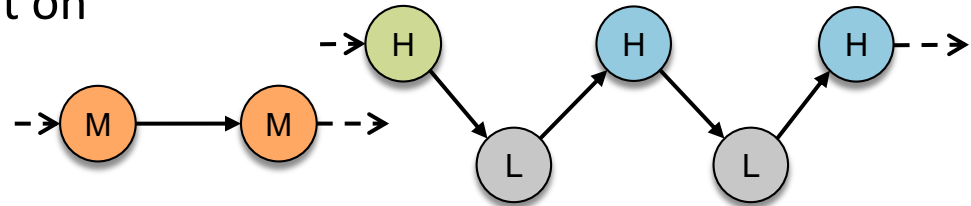
$$B_i(q) = \underbrace{q \sum_k C_{ik}^+}_{\text{self interference (bounded by } q\text{)}} + \underbrace{\sum_{j \neq i} \left( \sum_{j \in I_{ij}} \eta_j^+(B_i(q)) \cdot C_{jk}^+ + \sum_{k \in S_{ij}} C_{jk}^+ \right)}_{\substack{\text{normal interference} \\ \text{(bounded by } \eta_a^+ \text{)}}} \quad \underbrace{\sum_{k \in S_{ij}} C_{jk}^+}_{\text{critical deferred segment}}$$

inter-chain interference

# Application to asynchronous task chains

## Q-event task-chain busy window for asynchronous task chains:

- additional self-interference
  - deferred tasks  $D_{ij}$  = tasks dependent on a stalled task
- single-time blockers



inter-chain  
interference

$$B_i(q) = \boxed{\eta_i^+(B_i(q))} \sum_k C_{ik}^+ + \sum_{j \neq i} \left( \sum_{j \in I_{ij}} \eta_j^+(B_i(q)) \cdot C_{jk}^+ + \sum_{\boxed{k \in D_{ij}}} C_{jk}^+ \right)$$

self interference  
(bounded by  $\eta_b^+$ )

normal interference  
(bounded by  $\eta_a^+$ )

deferred tasks  
(bounded by 1,  
proof in the paper)



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# Related work

## Context-aware analysis extensions (distributed systems)

- offset-based analyses [Palencia et al. 1999, Redell 2003, Henia et al. 2006]
- pay bursts only once [Schliecker et al. 2009]
- limiting event streams [Kollmann et al. 2010, 2011]

## Refinement of task models

- classification and schedulability analysis [Stigge 2014]

➔no exploitation of (synchronous) communication semantics in chains on a single resource

# Experimental evaluation

## Implementation

- extension module for pyCPA
- requires small modification of pyCPA core (limit propagation)

## Experiments

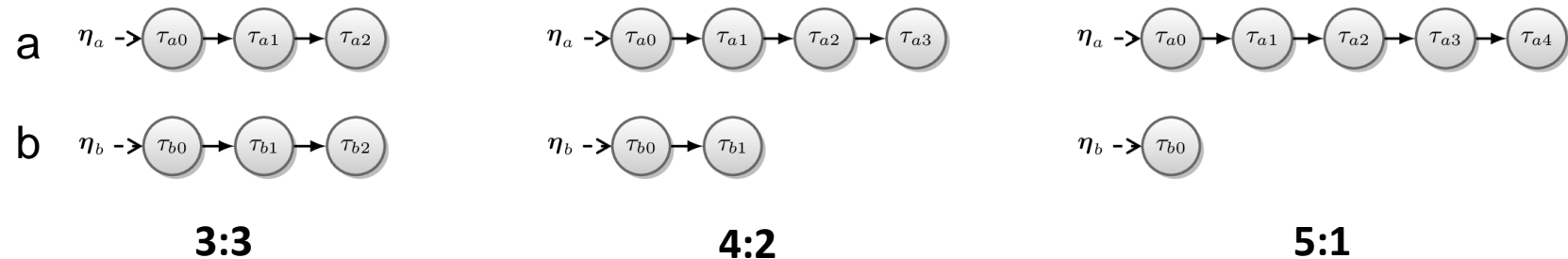
- **synthetic experiments**
  - conventional pyCPA (sum of tasks' WCRTs)
  - task-chain busy window
- **automotive use case (park assist + lane detection)**
  - conventional pyCPA (sum of tasks' WCRTs)
  - task-chain busy window
  - MAST (offset-based analysis with precedence relations)

pyCPA: <http://bitbucket.org/pycpa>  
MAST: <http://mast.unican.es/>

# Synthetic experiments – Setup

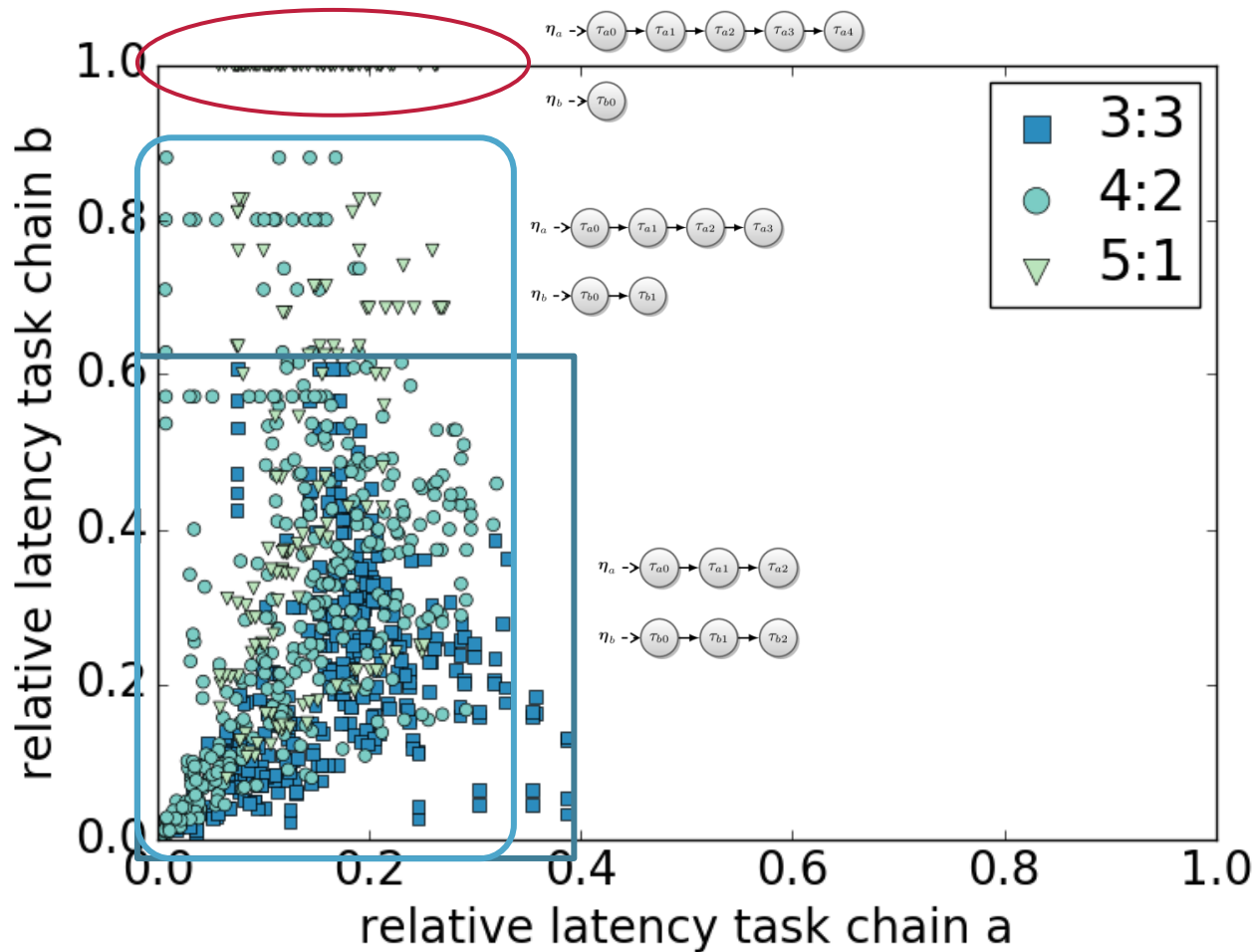
## Comparison of conventional pyCPA with our extension for task chains.

- task set of **six tasks** with fixed WCET/BCET
- three different compositions into **two chains (a & b)**



- utilisation:  $U_{3:3} = 0.97$  |  $U_{4:2} = 0.82$  |  $U_{5:1} = 0.78$
- distinct **task priorities**
- ran analysis for **all possible priority permutations** in each composition
- compared **resulting WCRTs** of both task chains

# Synthetic experiments – Synchronous



relative latency  
improvement:

**our results**

$$\frac{\text{task chain } WCRT}{\sum_i WCRT_i}$$

**conventional pyCPA**

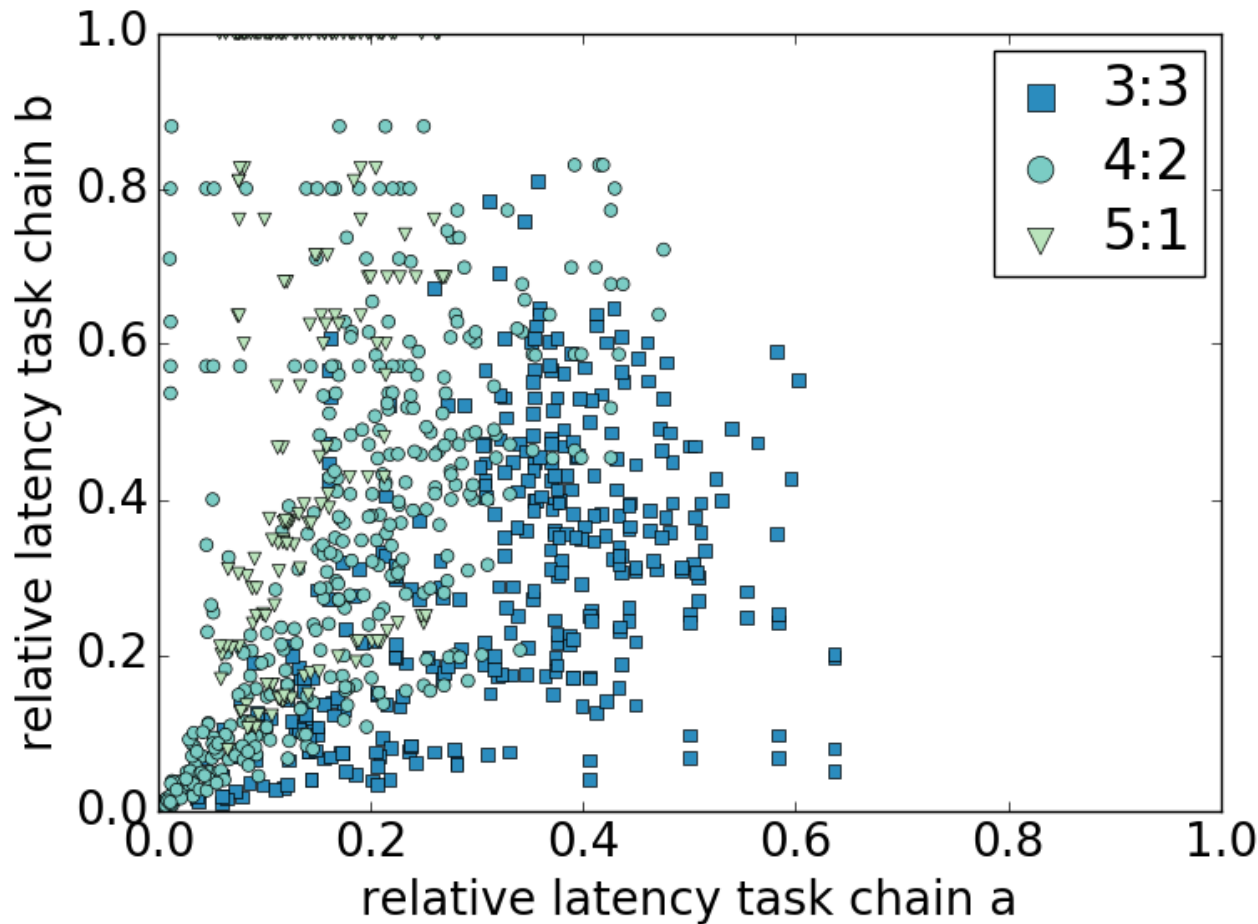
median improvement:

3:3) a: 0.18 | b: 0.19

4:2) a: 0.13 | b: 0.29

5:1) a: 0.13 | b: 0.6

# Synthetic experiments – Asynchronous

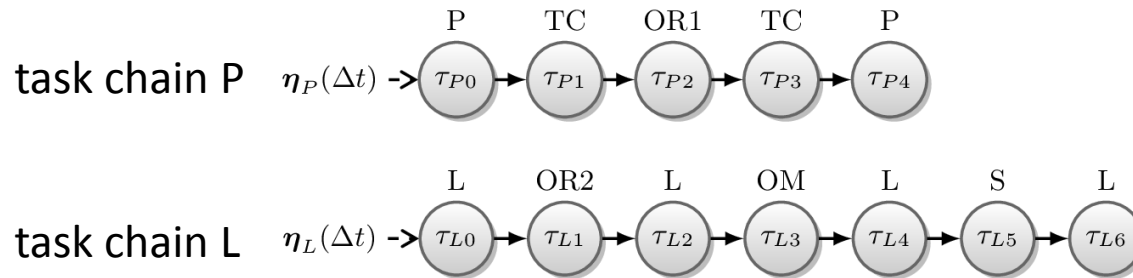


smaller improvement  
due to self-interference

median improvement:  
3:3) a: 0.35 | b: 0.29  
4:2) a: 0.17 | b: 0.33  
5:1) a: 0.13 | b: 0.6

# Automotive use case

## Parking assistant and lane detection (introductory example):



### Task chain P

- period 200ms, jitter 5ms, core execution time 70ms

### Task chain L

- period 100ms, jitter 5ms, core execution time 50ms

U=0.85

**Objective:** Find a feasible **thread priority** assignment under given **latency constraint** for both task chains (150ms).

→ analyse **5040 priority assignments**

# Automotive use case – Results summary

## Conventional CPA:

- analysed 5040 priority assignments in about **8h** (single core desktop)
- **no convergence** for all but 6 cases
- latency results between 4949 and 8613ms (P), 1017 and 2322ms (L)  
→ deemed **not feasible**

## MAST:

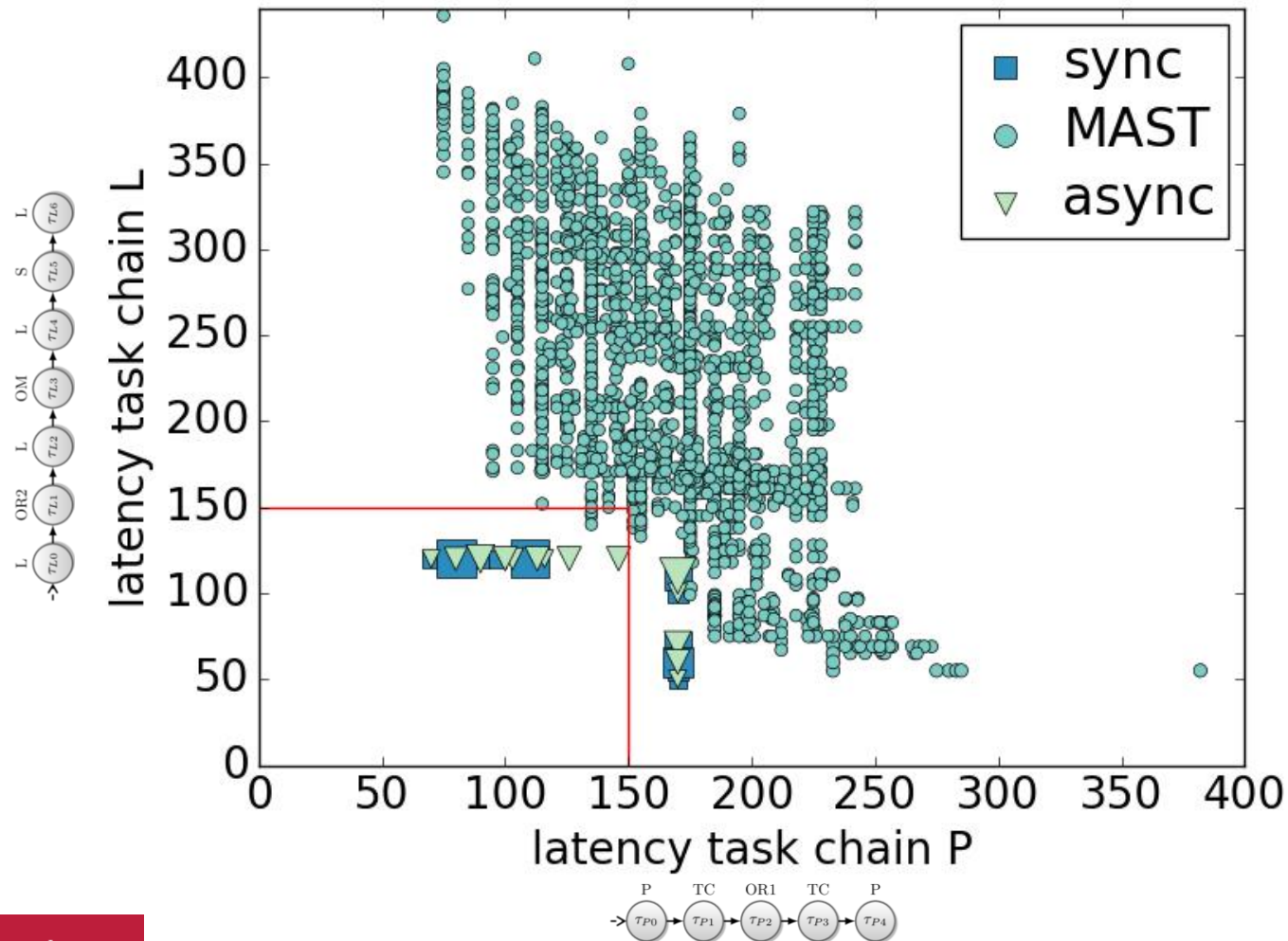
- analysis took **34 seconds**, results for **all** 5040 priority assignments
- **11** assignments **feasible** (below the required maximum latency)

## Task-chain busy window:

- analysis took **22 seconds**, converged for **all** 5040 priority assignments
- **2880** assignments **feasible** (below the required maximum latency)



# Automotive use case – Detailed latency results



# Summary & Conclusion

- Task chains resulting from **communicating threads** imply certain semantics.
- Improved **local scheduling analysis** for SPP-scheduled task chains.
- Improved **coverage** (# analysable systems).
- Much tighter (and realistic!) **WCRT results**.
- Reduced analysis **run-time** (from hours to seconds).
- Enables (in-field) **design-space exploration**.
- Enhances **applicability** of response-time analysis for existing software implementations (e.g. RTE, 3rd-party software stacks, libraries).

Thank you for your attention. Questions?

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